# HEMCHANDRACHARYA NORTH GUJARAT UNIVERSITY <br> PATAN-384265 

NAAC Accreditation Grade - "B"

## FACULTY OF SCIENCE

## MATHEMATICS

New Syllabus and Exam Scheme
B.Sc.

Semester - V \& VI

## With a Semester/ CBCS/Grading Pattern

 W.E.F. June -2013
## HEMCHANDRACHARYA NORTH GUJARAT UNIVERSITY, PATAN

| Programme code : | $V$ | Programme Name : | B.SC. |  |
| :--- | :--- | :--- | :--- | :---: |
| Faculty : | SCIENCE | Semesters : | V |  |
| Subject : | MATHEM ATICS |  |  |  |
| Effective from : | From Academic Year: 2013 -2014 |  |  |  |


| Sr. | Paper Code | Name of Paper | Credit |
| :---: | :---: | :---: | :---: |
| 1 | CC MATH-501 | Group Theory | 3 |
| 2 | CC M ATH-502 | M athematical Analysis - I | 3 |
| 3 | CC M ATH-503 | Differential Equations | 3 |
| Any One of the following |  |  |  |
| 4 | CC M ATH- 504 A <br> CC M ATH- 504 B <br> CC M ATH- 504 C | BOOLEAN ALGEBRA <br> Mechanics - I <br> Operations Research-I | 3 |
| 5 | $\begin{aligned} & \text { PC-M ATH } \\ & 501-504 \end{aligned}$ | PRACTICAL COURSES - MATLAB [PC 501, PC 502, PC503, PC504] | $1.5 \times 4=6$ |

UNIVERSITY, PATAN

| Programme code : | $v$ | Programme Name <br> $:$ | B.Sc. |
| :--- | :--- | :--- | :--- |
| Faculty : | SCIENCE | Semesters : | VI |
| Subject : | MATHEM ATICS |  |  |
| Effective from : | From Academic Year: 2013 -2014 |  |  |


| Sr. | Paper Code | Name of Paper | Credit |
| :---: | :---: | :---: | :---: |
| 1 | CC M ATH-601 | Abstract Algebra | 3 |
| 2 | CC M ATH-602 | M athematical Analysis - II | 3 |
| Any One of the following |  |  |  |
| 3 | CC M ATH- 603 A CC M ATH- 603 B | General Topology Number Theory | 3 |
| Any One of the following |  |  |  |
| 4 | CC M ATH- 604 A CC M ATH- 604 B CC M ATH- 604 C | GRAPH THEORY <br> M echanics II <br> Operations Research-II | 3 |
| 5 | $\begin{aligned} & \text { PC-M ATH } \\ & 601-604 \end{aligned}$ | PRACTICALCOURSES - MATLAB [PC 601, PC 602, PC603, PC604] | $1.5 \times 4=6$ |

## Hemchandracharya North Gujarat University. Patan. B.Sc. Semester: V \& VI Mathematics Syllabus (Effective from june-2013)

This syllabus is to be completed by assigning three period of one hour each and four practical of three hours each per week.
The number of students in a practical batch should not exceed twenty.

## PATTERN OF EXAMINATION :

They will be four paper for core compulsory and one paper for subject elective theory and six hours/day for two days per batch practical in the university examination. The pattern will be as follow.

| Written | Examination | Marks <br> External | Marks Internal |
| :--- | :--- | :--- | :--- |
| Core course-I | $\mathbf{3}$ hours | $\mathbf{7 0}$ | $\mathbf{3 0}$ |
| Core course-II | $\mathbf{3}$ hours | $\mathbf{7 0}$ | $\mathbf{3 0}$ |
| Core course-III | $\mathbf{3}$ hours | $\mathbf{7 0}$ | $\mathbf{3 0}$ |
| Core course-IV | $\mathbf{3}$ hours | $\mathbf{7 0}$ | $\mathbf{3 0}$ |
| Subject elective course | $\mathbf{2}$ hours | $\mathbf{5 0}$ | $\ldots . .$. |
| Laboratory course-I | $\mathbf{3}$ hours | $\mathbf{5 0}$ | $\ldots . .$. |
| Laboratory course-II | $\mathbf{3}$ hours | $\mathbf{5 0}$ | $\ldots . .$. |
| Laboratory course-III | $\mathbf{3}$ hours | $\mathbf{5 0}$ | $\ldots . . .$. |
| Laboratory course-IV | $\mathbf{3}$ hours | $\mathbf{5 0}$ | $\ldots . .$. |

## N.B.: Essential requirements for the MATLAB Practicals of Mathematical Subjects as CBCS has a high probability to be operationalised efficiently and effectively for the elevating learners.

1. Mathematical Laboratory inbuilt with sufficient number of Computers (as per the students enrollments and the number of practical batches) and MATLAB SOFTWARE with basic requirements for the MATLAB Practicals.
2. Mathematical Laboratory inbuilt with Graphs, Charts, Physical Models( two dimensional as well as three dimensional) \& Virtual Models ( Higher DDimensional - Computerized)) and basic requirements for the same.

# Hemchandracharya North Gujarat University. Patan. 

B. Sc. Programme<br>Semester-V<br>Mathematics : CC MATH-501<br>(Group Theory)

## UNIT : 1

Definition of a Group and illustrations, Elementary property of a Group, Equivalent definitions of a Group, Generalized form of Associative Law, Finite Groups and their tables, Definition of a Subgroup and illustrations, Lagranges theorem and its applications.

## UNIT: 2

Definition of a Permutation and illustrations, Transpositions and cycle, definition of a Normal subgroup and illustrations, Quotient group, Definition of an isomorphism of a group and its illustrations.

## UNIT: 3

Properties of a cycle groups, Isomorphism of cyclic groups, Subgroup of a cycle group, Generator of a cycle group, Definition of a Homomorphism and its illustrations, Kernel of Homomorphism, Cayley's Theorem, Isomorphism of group, Groups of order four and six.

The course is covered by the Book : I H Sheth, Abstarct Algebra, Prentice Hall of India (PHI) Publication. Chapter 6(6.1 to 6.7), Chapter 7(7.1 to 7.3), Chapter 8(8.1 to 8.3), Chapter 9(9.1 to 9.3), Chapter 10(10.1 to 10.2), Chapter 11(11.1 to 11.5), Chapter 12(12.1 to 12.6)

## Reference books:

1. I N Herstein, Topics in Algebra, Wiley Eastern Ltd.
2. N. Jacobson, Basic Algebra Vol I \& II, Hindustan Publishing company
3. Shanti Narayan, A text book of Modern Algebra, S. Chand \& Co.
4. P.B.Bhattacharya, S.K.Jain, S R Nagpal, Basics Abstract Algebra, (second Edition), Cambridge University Press.
5. N.S. Gopalkrishna, University Algebra, W iley Eastern, New Delhi
6. M aclane Saunders and Birkhoff Garrett, Algebra, M acM illan, New York.
7. G.F.Simmons, Introduction to Topology and Modern Analysis, M acGrawHill Inc., U.S.A.

## Mathematics: CC MATH-502

## Mathematical Analysis-I

Unit-1 Number System: The real field to be developed by ordered set approach, Equivalence of this approach and Dedikind's approach, Extended real number system, The complex number system, Euclidean spaces.

Unit-2 Basic Topology: Finite, Countable and Uncountable sets, Metric space, Neighborhoods in metric spaces, Limit point of a set, Open, Closed, Bounded, Compact, Perfect, Connected and Convex subsets of metric spaces.

Unit-3 Sequences and Series: Convergence sequence, Sub sequences, Cauchy sequences, Upper and lower limits, Special sequences and Series, Series of non negative terms, Roots and Ratio Test

Power Series with Real (Complex) terms, Interval (circle) of convergence and radius of convergence of a power series, Summation by parts, absolute convergence, addition and multiplication of series.

The course is roughly covered by Chapters 1,2,3 (Omit 3.52 to 3.55) of The book entitled "Principles of Mathematical Analysis" by Walter Rudin, McGraw Hill (International Student Edition), $3^{\text {rd }}$ Edition.

## Reference books:

(1) "A First Course in Mathematical Analysis" by D. Somasundaram \& B. Choudhary, Narosa Publishing House
(2) "Fundamentals of Mathematical Analysis" by G. Das \& S. Pattnayak Tata Mcgraw Hill Pub.Co
(3) "Fundamental of Real Analysis" by S. L. Gupta \& Nisha Rani - Vikas Pub. House Pvt. Ltd. New Delhi-1974.
(4) "Principle of Real Analysis "by S.C.Malik, Wiley Eastern Limited New Delhi 1982.

(6) "Principle of Mathematical Analysis" by T.M.Apostol

## Mathematics : CC MATH-503

## [DIFFERENTIALEQUATIONS]

Unit:1 Formation of Differential Equations, Symbolic Operator, Method of finding C.F., Sybolic Operator $1 / \mathrm{f}(\mathrm{D})$, Method of finding P.I., Shorter method of finding P.I., To find P.I. when $\mathrm{X}=\mathrm{e}^{\mathrm{ax}}$, where a is constant, To finding P.I. when $\mathrm{X}=$ Cosax or Sinax, To find the value of $1 / f(D) \cdot x^{m}$, where $m$ is positive integer, To find the value of $1 / f(D) \cdot\left(e^{a x} V\right)$, where $a$ is constant and V is a function of x . To evaluate $1 / \mathrm{f}(\mathrm{D}) .(\mathrm{XV})$, where V is a function of x . (Chapter:4)

Unit:2 Condition of Exactness of the linear differential equations, Solution of non-linear equations which are Exact, Equations of the form $y^{(n)}=f(x)$, Equations of the form $y^{(2)}=f(y)$, Equation do not contain $y$ directly, Equation that do not contain $x$ directly, Equation in which y appears in only two derivatives whose orders differ by two, Equation in which y appears in only two derivatives whose order differ by unity.(Chapter:6)

Unit:3 Method of solving $y^{(2)}+\mathrm{Py}^{(1)}+\mathrm{Qy}=\mathrm{R}$ when an integral included in the C.F. is known, Method of solving $\mathrm{y}^{(2)}+\mathrm{Py}^{(1)}+\mathrm{Qy}=\mathrm{R}$ by changing the dependent variable, $\mathrm{y}^{(2)}+\mathrm{Py}{ }^{(1)}+\mathrm{Qy}=\mathrm{R}$ by changing the independent variable, Solution by factorization of the Operator, Method of variation of Parameters, Method of Undetermined Co-efficient.(Chapter:7)

The course is covered by "A text book of Differential Equations", by N.M.Kapoor, Pitamber publication, New Delhi.

## REFERENCE BOOKS:

1. Erwin Kreyszing, Advanced Engineering mathematics, By. John Wiley \& Sons Inc. New York, 1999.
2. D.A.Murray, Introductory course on Differential Equations, By. Orient Longman,(India), 1967.
3. A.R.Forsyth, A Terastise on Differential Equations, Macmillan and Co.Ltd., London.
4.Ian N. Sneddon, Elements of partial Differential Equations, McGraw-Hill Book Compony, 1998.
4. Fracis B. Hilderbrand, Advanced Calculus for Application, Prentice Hall of India Pvt. Ltd., New Delhi, 1977.
5. Jane Cronin, Differential Equations, Marcel Dekkar, 1994.
6. Frank Ayres, Theory and Problems of Differential Equations, McGraw-Hill Book Compony, 1972.

## Mathematics : CC MATH-504 A

## BOOLEAN ALGEBRA

UNIT:1 Relations ,Equivalence Relation,Equivalance classes or sets,Partial order Relations,Hasse Diagram,Upper and Lower Bounds,Minimal and Maximal elements ,Binary operations,closure operations,Partially Ordered Set,Totally Ordered Set,Lattices as Posets,Dual Lattice,Meet and Join,Lattice as an algebraic structure,Direct Product Of two Lattices,Lattice Homomorphism,Lattice Isomorphism.

UNIT:2 Sub-Lattice,Completed Lattice,Bounded Lattice,Distributive
Lattice,Square Free Lattice,Complemented Lattice,Modular Lattice,De Morgan's Law,BooleanAlgebra,Boolean Algebra of Switching Circuits,Sub Boolean Algebra,Homomorphism and Isomorphism of Boolean Algebras,Atoms,Unique representation Theorem,Properties Of Set of Atoms,Stone's representation Theorem.

UNIT:3 Boolean Variables,Boolean Expression,Min term,Maxterm,Representation of Boolean Expression as a sum of Product Cannonical Form and as aProduct of Sum Cannonical Fofm,Boolean Function Associated With Boolean Expression,Symmetric Boolean Expression,Represantation of Boolean Functions And Minimization of Boolean Expression:Using Truth Table,Cube array Method,Karnaugh's Method,Circuit Diagrams.

REFERENCE BOOKS:
1.An Introduction To Discrete Mathematics -Udayan M.Prajapati, Dr.Ajay S. Gor, Nirav Prakashan
2.Discrete Mathematical Structures With Applications to Computer Science by Trembley I.P.AndMahonar R.
3.Discrete Mathematical Structures With applications to Computer Science by R.Hamming and E.A.Feigenbaum
4.Discrete Mathematical Structures for Computer Science by B.Kolman and R.C.Busy
5.The Essence of Discrete Mathematics by Neville Dean

# Mathematics: CC MATH-504 B <br> Mechanics-I 

UNIT-1 Method of Plane Statics:

Fundamental for Newtonian Mechanics, Scalar field, Gradient Vector, Equilibrium of a particle and system of particles.

## UNIT- 2

Necessary and Sufficient conditions for Equilibrium, Equipollent system of forces. Reduction of general force system. Principles of virtual work and potential energy.

## UNIT-3

Mass centre of system of particles, Potential energy, Friction, Flexible Cables.

## REFERENCE BOOKS :

1. Synge and Griffith: Principal of Mechanics
2. S.L.Loney : Statics,Macmillan and company, London.
3. R.S.Verma : A Text book on Statics,Pothishala Pvt. Ltd., Allahabad.
4. S.L.Loney : An elementary treatise on the Dynamics of a particle and rigid bodies.,Cambridge University press 1956.

5 Mechanics : Dr. L.K.Patel.

# Mathematics : CC MATH-504 C OPERATIONS RESEARCH - I 

Unit-1. Introduction: Nature and scope of Operations Research.
Linear programming: (a) LP Model and method of solution- Graphical method, Slack-Surplus and unrestricted variables, Simplex Algorithm, Simplex Method.

Unit-2 . Artificial Slack variables, Two phase method, Big-M / Penalty method, Variation in simplex method solution- unbounded, infeasible solutions and concept of degeneracy.

Unit-3. (a) Duality Theory-
The essence of duality theory, primal-dual relationships, Duality theorems, Dual simplex method.
(b) Integer Programming- The need of integer solutions, The concept of the Cutting - Plane, Gomory's Cutting Plane Algorithm, Branch and Bound Method (sums of $B \& B$ not to be asked in the exam.)

## REFERENCES BOOKS:

(1) Operations Research , by. J.K.Sharma. Macmillan Publishers India Ltd.
(2) Operations Research by Nita Shah, Ravi Gor and Hardik Soni, Prentice Hall of India.
(3) Operations Research( Principles and Practice) by Pradeep Prabhakar Pai, Oxford University Press.

## Mathematics : PC MATH-501-504

## Objectives:

- Understand the MATLAB Desktop, Command window and the Graph Window
- Be able to do simple and complex calculation using MATLAB
- Understand the graphics capabilities of MATLAB
- Be able to carry out mathematical computations using MATLAB Symbolic Toolbox


## PCMAT-501

## Introduction to MATLAB

Starting and ending MATLAB session, MATLAB environment, MATLAB help, types of files, search path, some useful MATLAB commands, data types, constant and variables, operators, built-in functions, assignment statement, illustrative programs.

## Vectors and Matrices

Scalars and vectors, entering data in matrices, line continuation, matrix subscripts/indices, multi-dimensional matrices and arrays, matrix manipulations, generation of special matrices, useful commands, matrix and array operations, function with array inputs.

## PCMAT-502

## Polynomials

Entering a polynomial, polynomial evaluation, roots of a polynomial, polynomial operations - addition and subtraction, multiplication, division, formulation of polynomial equation, characteristic polynomial of a matrix, polynomial differentiation, integration, and curve fitting, evaluation of polynomial with matrix arguments.

## PCMAT-503

## MATLAB Graphics:

Two-dimensional plots, multiple plots, style options, legend command, subplots, specialized two-dimensional plots, three-dimensional plots.

## PCMAT-504

## Symbolic Processing With MATLAB

Symbolic Expressions and Algebra, Algebraic and Transcendental Equations, Calculus, Symbolic Linear Algebra, ordinary and partial differential equation, Symbolic Tutors.

## Text Book:

1. "MATLAB and its Applications in Engineering" Raj Kumar Bansal, Ashok Kumar Goel, Manoj Kumar Sharma, Pearson.

## coverage from the Text Book:

## PCMAT-501

Chapter 1: 1.8, Chapter 2: 2.9 Chapter 3: 3.11

## PCMAT-502

Chapter 4: 4.13

## PCMAT-503

Chapter 6: 6.8

## PCMAT-504

Chapter 9: 9.3 only. Additional commands for symbolic toolbox are to be covered from the list given below.

## Symbolic Math Toolbox

| Functions for Creating and Evaluating Symbolic Expressions |  |
| :--- | :--- |
| class | Returns the class of an expression. |
| digits | Sets the number of decimal digits used to do variable precision arithmetic. |
| double | Converts an expression to numeric form. |
| ezplot | Generates a plot of a symbolic expression. |
| ezplot3 | 3-D parametric plot |
| ezpolar | plot a 2-D curve in polar coordinates |
| findsym | Finds the symbolic variables in a symbolic expression. |
| numden | Returns the numerator and denominator of an expression. |
| sym | Creates a symbolic variable. |
| syms | Creates one or more symbolic variables. |
| vpa | Sets the number of digits used to evaluate expressions. |


| Functions for Manipulating Symbolic Expressions |  |
| :--- | :--- |
| collect | Collects coefficients of like powers in an expression. |
| expand | Expands an expression by carrying out jpowers. |
| factor | Factors an expression. |


| poly2sym | Converts a polynomial coefficient vector to a symbolic polynomial. |
| :--- | :--- |
| pretty | Displays an expression in a form that resembles typeset mathematics. |
| simple | Searches for the shortest form of an expression. |
| simplify | Simplifies an expression using Maple's simplification rules. |
| subs | Substitutes variables or expressions. |
| sym2poly | Converts an expression to a polynomial coefficient vector. |

## Symbolic Calculus Functions

| diff | Returns the derivative of an expression. |
| :--- | :--- |
| jacobian | Compute the Jacobian matrix. |
| Dirac | Dirac delta function (unit impulse). |
| Heaviside | Heaviside function (unit step). |
| int | Returns the integral of an expression. |
| limit | Returns the limit of an expression. |
| symsum | Returns the symbolic summation of an expression. |
| taylor | Returns the Taylor series of a function. |

## Symbolic Linear Algebra Functions

| det | Returns the determinant of a matrix. |
| :--- | :--- |
| eig | Returns the eigenvalues (characteristic roots) of a matrix. |
| inv | Returns the inverse of a matrix. |
| poly | Returns the characteristic polynomial of a matrix. |

## Symbolic Tutors

| arclen | Find the arclength of the curve. |
| :--- | :--- |
| composefun | compose two functions |
| dirdifftool | plot or animate directional derivatives |
| eigtool | interactive matrix eigenvalues |
| gradtool | plot or animate gradient(s) |
| linsys | plot a system of 2-D or 3-D linear equations |
| ratfun | demonstrate the graphing of rational functions |
| rsums | Riemann sum approximate integration tutor |
| taylortool | taylor approximation tutor |

Assignment: The student should submit the electronic copy of diary file showing the execution/output of Matlab session(s).

# B. Sc. Programme <br> Semester-VI <br> Mathematics : CC MATH-601 <br> <br> (Abstract Algebra) 

 <br> <br> (Abstract Algebra)}

## UNIT : 1

Definition of a Ring and illustrations, Propertis of a Ring, Zero divisors and Integral domain, Characteristic of an Integral Ring, Solution of the equation $a x=b$ in a ring R, Subrings, Ideals,

## UNIT : 2

Introduction of Polynomials, Integral Domain $\mathrm{D}[\mathrm{x}]$, Familiar form of Integral domain $\mathrm{D}[\mathrm{x}]$, Unique factorization of Polynomials, Solutions of a Polynomial Equation, Eisenstein Criterion for irreducibility.

## UNIT : 3

Quotient ring, Homomorphism of rings, M aximal Ideal, Prime Ideal,
The course is covered by the Book : I H Sheth, Abstarct Algebra, Prentice Hall of India (PHI) Publication. Chapter 13(13.1 to 13.4), Chapter 14(14.1 to 14.4), Chapter 15(15.1 to 15.4), Chapter 16(16.1 to 16.3), Chapter 18(18.1 to 18.7), Chapter 19(19.1 to 19.4),

## Reference books:

1. I N Herstein, Topics in Algebra, Wiley Eastern Ltd.
2. N. Jacobson, Basic Algebra Vol I \& II, Hindustan Publishing company
3. Shanti Narayan, A text book of Modern Algebra, S.Chand \& Co.
4. P.B.Bhattacharya, S.K.Jain, S R Nagpal, Basics Abstract Algebra, (second Edition), Cambridge University Press.
5. N.S. Gopalkrishna, University Algebra, W iley Eastern, New Delhi
6. M aclane Saunders and Birkhoff Garrett, Algebra, MacM illan, New York.
7. G.F.Simmons, Introduction to Topology and Modern Analysis, M acGrawHill Inc., U.S.A.

## Mathematics : CC MATH-602

## Mathematical Analysis-II

Unit-1 Limits and Continuity: Limits and Continuity for a functions from a metric space into another metric space, continuity of a composite function, Structural properties of continuous functions from a metric space in to $\mathrm{R}^{\mathrm{k}}$, Continuity and Compactness, Continuity and connectedness, Discontinuities, Monotonic function, Discontinuities of a monotonic function, Infinite limits and limits at infinity.

Differentiation: Derivatives of a real function, Continuity and differentiability, Structural properties of the class of differentiable functions, Mean value theorems, Continuity of derivatives, L'Hospital rule, Derivatives of higher order, Taylor's theorem.

Unit-2 The Riemann - Stieltje's Integral: Riemann integral and Stieltje's integral, properties of Riemann integral and Stieltje's integral, Integration and Differentiation, Integration of Vector Valued Functions, Rectifiable curves.

Unit-3 Sequences and Series of functions: Sequences of functions, Limit of a Sequence of functions, Uniform convergence, tests for uniform convergence and continuity, Uniform convergence and differentiation.

The course is roughly covered by Chapters - 4,5,6,7 (Omit 5.16 to 5.20 and 7.28 to 7.33) of The book entitled "Principles of Mathematical Analysis" by Walter Rudin, McGraw Hill (International Student Edition), $3{ }^{\text {rd }}$ Edition.

## Reference books:

(1) "A First Course in Mathematical Analysis" by D. Somasundaram \& B. Choudhary, Narosa Publishing House.
(2) "Fundamentals of Mathematical Analysis" by G. Das \& S. Pattnayak Tata Mcgraw Hill Pub.Co
(3) "Fundamental of Real Analysis" by S. L. Gupta \& Nisha Rani - Vikas Pub. House

Pvt. Ltd. New Delhi-1974.
(4) "Principle of Real Analysis "by S.C.Malik, Wiley Eastern Limited New Delhi 1982.

(6) "Principle of Mathematical Analysis" by T.M.Apostol

# Mathematics : CC MATH-603 A General TOPOLOGY 

Unit-1. Toplology and topological spaces, Neighbourhoods, Hausdorff space, Closure of a subset of a topological space.

Unit-2. Interior of a subset of topological space , Boundary of a subset of a topological space, Continuity of a function from topological space to topological space, Hoeomomorphism between two topological spaces.

Unit-3. Subspace of a topological space, Connectedness of a topological spaces, Some applications of connectedness, Components of a point of connected topological space.

Text-Book: An Introduction to topology, by. Bert M endelson(third addition)
Ch.No.-3: 2.1 to $2.4,3.1,3.3,3.7,4.2$ to $4.15,5.1$ to $5.7,5.9,6.1$ to $6.3,6.5$ to 6.8
Ch.No.-4 : 2.1 to $2.7,4.1$ to $4.3,5.1$ to 5.7

## REFERENCE BOOKS:

(1) Introduction to Topology and Modern Analysis, by. "G F Symmons"., New York M cGraw Hill, 1963
(1) General Topology by Kelly J L , NewYork, Van Nostrand 1955
(3) Elementary Topology by Beackett D W., New York Academic press, 1967

## Mathematics : CC MATH-603 B

## Number Theory

## Unit I:

Some Preliminary Consideration: Well-Ordering Principle, Mathematical Induction, the Binomial Theorem \& binomial coefficients.
Divisibility Theory: the division algorithm, divisor, remainder, prime, relatively prime, the greatest common divisor, the Euclidean algorithm (Without proof), the least common multiple, the linear Diophantine equation \& its solution.

## Unit II:

Prime Numbers: Prime and composite number, the Fundamental Theorem of Arithmetic (without proof), canonical form of a number, the Sieve of Eratosthenes.
Theory of Congruence: Definition and basic properties of congruence, Residue class \&complete system of residues, special divisibility test, linear congruence, Chinese Remainder Theorem. (without proof)

## Unit III:

Fermat's Theorem: Fermat's Factorization method, Fermat's little theorem, Wilson theorem, Euler's theorem: Euler's Phi-function () $n \varphi$ and formula for() $n \varphi$, Euler's theorem (without proof) and only problems on Euler's theorem.

## Text Book:

Elementary Number Theory - David M. Burton, Sixth Edition, Universal Book stall, New Delhi.
[(Chapter 1): 1.1 and 1.2 2) 2.1 to 2.4 3) 3.1 and 3.2 4) 4.1 to $4.3 ~ 5) 5.2$ and $5.3 \quad$ 7) 7.2 and 7.3 ]

## Reference Books:

1 An introduction to the Theory of numbers - Niven and Zuckerman, Wiley Eastern Ltd.
2 Number Theory - S. G. Telang, Tata Mc Graw-Hill Publishing Company Limited, New Delhi
3 Elementary Theory of Numbers - C. Y. Hsiung, Allied Publishers Ltd.-India, ISBN 81-7023-464-6.
4 Number Theory - George E. Andrews, Hindustan Publishing Corporation- Delhi.
5 Elementary Number Theory - Gareth A. Jones \& J. Mary Jones, Springer Verlag, ISBN 81-8128-278-7.
6. Number Theory - J. Hunter, Oliver and Boyd-London.
7. Beginning Number Theory - Neville Robbins, Narosa Pub. House -New Delhi ISBN 978-81-7319-836
8 Introduction to the theory of Numbers - G. H. Hardy \& E. M. Wright, Oxford Uni. Press
9 Higher Algebra - S. Barnard \& J. M. Child, Macmillan India Ltd
10 Elements of Number Theory - I. M. Vinogradov, Dover Pub INC
11 Elementary Number Theory in Nine chapters - James J. Tattersall, Cambridge Uni Press
12 A first course in Theory of Numbers - K. C. Chowdhary, Asian Books Pvt Ltd New Delhi
131001 problems in Classical Number Theory - Jean Marie De Konick Armed Mercier, AMS

## Mathematics : CC MATH-604 A

GRAPH THEORY
UNIT:1 Graphs,Basic Definitions,Undirected Graphs,M ixed W eighted Graphs,Incidence and Degree,Bipartite Graph and Bipartition,Regular and K-regular Graph,Graph Isomorphisms,Sub Graphs,Graph Operations,Walk,Trail,Paths ,Circuits,Connected Graph,Disconnected Graph,Eccentricity,Radius and Diameter,Adjacency Strong ,W eak and Unilateral Components,Eular Graphs,Hamilton Paths,Trees,Binary Trees And m-arrayTree,Spanning Trees.

UNIT:2 Cut set,Internaly Disjoint Paths, Connectivity and Separability,Planar Graphs and their different Representation, Detection Of Planarity,Geometric and Combinatorial duals,Vector Space Associated With a Graph.Circuit and Cut set Subspaces ,Orthogonal Vectors And spaces.

UNIT:3 Incidence M atrix,Adjancy M atrix Of a Graph.Path matrix and their reletion ships. Colouring of a Graph,Chromatic Number,Chromatic Partitioning,Covering. Acyclic digraphs and dia cyclizations.

REFERENCE BOOKS:
1.An Introduction To Discrete Mathematics -

Udayan M.Prajapati Dr.Ajay S. Gor, Nirav Prakashan
2.Graph Theory with Applications toEngineering and Computer Science by Narsing Deo 3.Discrete M athematical Structures With Applications to Computer Science by Trembley I.P.AndM ahonar R.
4. Graph Theory by Harary F.
5. Graph Theory and its applications by B. Harris
5.Discrete M athematical Structures With applications to Computer Science by R.Hamming and E.A.Feigenbaum
4.Discrete M athematical Structures for Computer Science by B.Kolman and R.C.Busy
5.The Essence of Discrete M athematics by Neville Dean

# Mathematics: CC MATH-604 B 

## Mechanics-II

## UNIT-1

Plane Kinematics, Tangential and Normal components of velocity and acceleration, Radial and tranverse components. M otion of a rigid body parallel to a plane. Linear momentum and conservation of energy for a particle and for a system of particles. Projectile without resistence.

## UNIT-2

Harmonic Oscillators. General motion under central force and Central Orbits, Planetary Orbits. Kepler's laws of motion.

## UNIT-3

Moment of inertia. Kinetic energy and angular momentum. Rotation of a rigid body about a fixed axis.

General motion of a cylinder parallel to a fixed plane. Compound pendulum. Plane impulsive motion. Impulsive force. Principle of linear and angular momentum. Collision of sphere and coefficient of restitution. Examples.

## REFERENCE BOOKS:

(1) Synge and Griffith: Principal of Mechanics
(2) S.L.Loney : Statics,Macmillan and company, London.
(3 )R.S.Verma : A Text book on Statics,Pothishala Pvt. Ltd., Allahabad.
(4) S.L.Loney : An elementary treatise on the Dynamics of a particle and rigid bodies.,Cambridge University press 1956.
(5) Mechanics : Dr. L.K.Patel.

# Mathematics : CC MATH-604 C <br> Operations Research II 

Unit-1. Network Models- Concept of Networks.
Transportation Problem- Introduction, general method of a T.P., unbounded T.P. NWCM, Least cost method, VAM methods to find the initial solution, Dual of a T.P. and MODI method, degeneracy in a T.P., variatons in T.P.- Maximization T.P. and prohibited routes.
Assignment Problem- General model of A.P.(A.P. as a special case of a T.P.) Hungarian Method of solving a A.P., variations in a A.P.- maximization, prohibited assignments.

## Unit-2. Sequencing Problem :

Methods of sequencing, Johnson's Algorithm for a two machine problem, three machine problem and M-machine problem, Processing Two jobs through Mmachines
Unit-3. Game Theory: Introduction, Two-person zero games, Minimax and Maximax principles, saddle point theorems, mixed strategies, method for solution of $2 \times 2$ game, dominance principles, solution of games without sadddle points by using dominance and then mixed strategies, graphical method of solving $2 \times \mathrm{m}$ and $\mathrm{m} \times 2$ game, L.P. solution of games.

## REFERENCES BOOKS:

(1) Operations Research , by. J.K.Sharma. Macmillan Publishers India Ltd.
(2) Operations Research by Nita Shah, Ravi Gor and Hardik Soni, Prentice Hall of India.
(3) Operations Research( Principles and Practice) by Pradeep Prabhakar Pai, Oxford University Press.

## Semester-VI <br> Mathematics : PC MATH-601-604

## Objectives:

- Ensure the student can competently use the MATLAB programming environment
- Understand the capabilities of MATLAB for solving complex mathematical problems
- Understand the tools that are essential in solving real-world problems applying appropriate Mathematical concept.


## PCMAT-601

## Input-Output Statements in MATLAB

Data input, interactive inputs, reading/storing file data, output commands, formatted input-output functions.

## PCMAT-602

## Programming Techniques

Loops, Branches control structures, MATLAB programming, function subprograms, types of functions, function handles, errors and warnings, MATLAB debugger.

## PCMAT-603

## MATLAB Applications:

The content of this unit is to be covered from the list given in Appendix A.

## PCMAT-604

## Practical using MATLAB programming

List of practical is given in Appendix B.

## Text Book:

"MATLAB and its Applications in Engineering" Raj Kumar Bansal, Ashok Kumar Goel, Manoj Kumar Sharma, Pearson.
coverage from the Text Book:
PCMAT-601
Chapter 5: 5.6
PCMAT-602
Chapter 7: 7.3, Chapter 8: 8.9

## PCMAT-603

Appendix A: Table A.1:A. 8
PCMAT-604

## Appendix B

## Appendix A:

Table A. 1

Discrete MathlNumber theoretic functions

| factor | Returns Prime factors |
| :--- | :--- |
| factorial | Factorial function |
| nchoosek | All combinations of N elements taken K at a time |
| perms | All possible permutations |
| gcd | Returns the greatest common divisor. |
| lcm | Returns the least common multiple. |
| primes | Generate list of prime numbers |
| isprime | Returns a logical array that is prime numbers. |
| rat, rats | Returns a rational fraction approximation. |
| mod | The mod function is useful for congruence relationships. Returns modulus after |
| rem | Returns remainder after division. |

Table A. 2

Coordinate System Conversion

| cart2sph | Transform Cartesian to spherical coordinates |
| :--- | :--- |
| cart2pol | Transform Cartesian to polar coordinates |
| pol2cart | Transform polar to Cartesian coordinates |
| sph2cart | Transform spherical to Cartesian coordinates |

Table A. 3

## Interpolation Functions

| interp1 | Linear and cubic-spline interpolations of a function of one variable. |
| :--- | :--- |
| interp2 | Linear interpolation of a function of two variables. |
| spline | Cubic-spline interpolation. |
| unmkpp | Computes the coefficients of cubic-spine polynomials. |

Table A. 4

| Numerical Integration Functions |  |
| :--- | :--- |
| quad | Numerical integration with adaptive Simpson's rule. |
| quadl | Numerical integration with adaptive Lobatto quadrature. |
| trapz | Numerical integration with the trapezoidal rule. |
| quadv | Vectorized quadrature |
| dblquad | Numerically evaluate double integral |
| triplequad | Numerically evaluate triple integral |

Table A. 5

| Numerical Differentiation Functions |  |
| :--- | :--- |
| diff(x) | Computes the difference between adjacent elements in the vector x. |
| polyder | Differentiates a polynomial, a polynomial product, or a polynomial quotient. |

Table A. 6

| ODE Solvers |  |
| :---: | :---: |
| ode23 | Nonstiff, low-order solver. |
| ode45 | Nonstiff, medium-order solver. |
| ode113 | Nonstiff, variable-order solver. |
| ode23s | Stiff, low-order. |
| ode23t | Moderately stiff, trapezoidal rule solver. |
| ode23b | Stiff, low-order solver. |
| ode15s | Stiff, variable-order solver. |
| odeset | Creates integrator options structure for ODE solvers. |
| deval | Evaluate solution of differential equation problem |
| bvp4c | Solve boundary value problems for ODEs |

Table A. 7

| Optimization |  |
| :--- | :--- |
| fminbnd | Finds minimum of single-variable function. |
| fzero | Finds zero of single-variable function. |
| fminsearch | Multidimensional unconstrained nonlinear minimization |
| lsqnonneg | Linear least squares with nonnegativity constraints |
| fminunc | Find minimum of unconstrained multivariable function |


| fmincon | Find minimum of constrained nonlinear multivariable function |
| :--- | :--- |
| linprog | Solve linear programming problems |

Table A. 8

| Statistical Functions |  |
| :--- | :--- |
| $\operatorname{erf}(\mathrm{x})$ | Computes the error function $\operatorname{erf}(\mathrm{x})$. |
| mean | Calculates the average. |
| median | Calculates the median. |
| std | Calculates the standard deviation. |
| var | Calculates the variance. |
| corrcoef | Correlation coefficients |
| cov | Covariance matrix |

## Appendix B:

1. Numerical Methods Practical (Lab) using MATLAB programming
2. Linear Algebra
3. Graph Theory
4. Calculus
5. Optimization
6. Problems related to programming given in text book.

Assignment: The work should involve programming using MATLAB. The student should submit the electronic copy of .m files or/and diary file showing the execution/output of Matlab session(s).

## PATAN-384265

## FACULTY OF SCIENCE

B.Sc. for Semester - I \& VI

With a Semester/ CBCS/Grading Pattern Subject Elective Courses (Each of 2 Credit)

## List of Subject Elective Courses

EC-I : Computer C Language
EC-II: Industrial M athematics-1
EC-III: Industrial M athematics-2
EC-IV: Business M athematics-1
EC-V Business M athematics-2
( Detailed Syllabus of EC-I to EC-V submitted to the University)

## Detailed Syllabus of New Subjective Elective Courses

to be implemented from June-2012
EC-VI : Business Mathmatics-3
EC-V : Business Mathmatics-4

## Subject Elective Course : EC-VI

## Business M athematics-3

Unit:1 [Differential Calculus] [only examples]
Definition of differentiation in one variable, Working rules of differentiation, Derivative of $\mathrm{x}^{\mathrm{n}}, \log \mathrm{x}, \mathrm{e}^{\mathrm{x}}, \mathrm{a}^{\mathrm{x}}$, trigonometric functions and inverse trigo. Functions, Differentiation of method of substation and implicit function, parametric equations, Diff. of $f(x)^{g(x)}$.
Unit:2 [Integral Calculus] [only examples]
Indefinite integral: Definition, Working rules of integration, integration of $x^{n}, a^{x}, e^{x}$, integration of $\frac{1}{x^{2} \pm a^{2}} ; \frac{1}{\sqrt{x^{2} \pm a^{2}}} ; \frac{1}{\sqrt{a^{2}-x^{2}}} ; \frac{1}{|x| \sqrt{x^{2}-a^{2}}}$ integration of
trigonometric functions, integration by method of substitution, Some standard results: $\int f(x) d x=F(x)+c \Rightarrow$

$$
\begin{aligned}
& \int f(a x+b) d x=\frac{1}{a} F(a x+b)+c, \int[f(x)]^{n} \cdot f^{\prime}(x) d x, \int \frac{f^{\prime}(x)}{f(x)} d x \\
& \int \frac{1}{a x^{2}+b x+c} d x, \int \frac{1}{\sqrt{a x^{2}+b x+c}} d x .
\end{aligned}
$$

## Referance books:

(1) Business M athematics
by. D.C.Sancheti \& V.K.Kapoor, Sultan Chad \& Sons Publication, New Delhi.
(2) Business M athematics
by. B.S.Shah Prakashsan, Ahmedabad.
(3) Any Advance Calculusbooks used in Science Streme .

## Subject Elective Course : EC-VII

## Business M athematics-4

Unit:1 Logic: [only examples] Logical Statements, Truth table, Negation, Compound statements, Tautologies and Contrdiction, Negation of Compound statements, Propositions, Conditional and Biconditional statements.

Set Theory: [only examples]
Definition and methods of sets, types of sets, Venn diagrams, Operation s on sets, De-M organ's law, Finite and infinite sets.

## Unit:2 Permutations and Combinations: [only examples]

Fundamental rules of counting, Definition of Permutations and Permutation of $n$ different things, Permutation of repeated things, Circular Permutation, Definition of Combination standard results and examples.

## Referance books:

(1)Business Mathematics. BY. D.C.Sancheti \&
V.K.Kapoor,

Sultan Chad \& Sons Publication, New Delhi.
(2) Business Mathematics.
by. B.S.Shah Prakashsan, Ahmedabad.

